

Rigidity results in linearized elasticity with cracks

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Some non-exhaustive bibliographic references

Measures, Hausdorff measures, functions with bounded variations, area and co-area formula: [3, 21, 22, 23, 29].

Mumford-Shah problem, compactness, weak minimizers are strong: [32, 1, 20, 18, 31].

Griffith model: [24, 6].

Korn, BD , “ $GSBD$ ”: [33, 4, 2, 5, 15, 13, 17, 14] (Historical: [34, 30, 36, 35]).

Rigidity in $GSBD$: [27, 26, 9, 7].

Existence for Griffith: [12, 16, 10, 11].

Quasistatic growth of fracture: [19, 8, 25, 28].

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